

## **Development and Implementation of a Washout Algorithm for a 6-dof Motion Platform of Flight Simulator**

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**ABSTRACT:** *Flight simulators for pilot training is extremely important due safety and economic factors. Flight simulator needs to simulate different kinds of complicated motion state such as roll, pitch and yaw angles. It has six-degree of freedom, high precision, high rigid, modular design and many other advantages. The motion system responds to the aircraft linear and angular accelerations in order to compute the most appropriate cabin motion to replicate these accelerations, subject to the displacement limits and the velocity limits of the actuators. The cabin accelerations are filtered in order to compute the most appropriate cabin motion to replicate the actual airplane accelerations. This paper developed and implemented a motion washout algorithm that can enhance the fidelity of motion platform and the cabin motion never exceeds the mechanical limits of the motion platform, particularly the maximum actuator displacements and the maximum actuator velocities.*

**Keywords:** *Motion washout algorithm, Flight Simulator, 6-dof motion platform, Simulation fidelity*

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### **I. INTRODUCTION**

Currently, parallel motion platform has been studied and applied widely result from its advantages in terms of rigidity, accuracy, simple structure and ability of large load bearing. Lots of various advantages have been discussed in the research literature [1]. Because of its obvious asset the 6-dof parallel motion platform has been used on flight simulator. A flight simulator has two most important functions, one is flight training the other is research and development [2]. A flight simulator must provide linear motion along the three axis and angular motion around the three axes of the plane to the pilot. The 6-dof parallel motion platform will make the motion such as pitching, yawing, rolling, acceleration, deceleration, and even turbulence, so it can simulate the motion of a real plane.

Motion washout algorithm [3] can limit motion range of a flight simulator within a physical limitation of the 6-dof parallel motion platform. This paper proposed a novel motion washout algorithm that can accurately transform aircraft specific force into flight simulator platform motions at high fidelity within the flight simulator's physical limitations.

It is important to design reasonable washout algorithms to replicate real aircraft sensations for pilots in limited space as accurately as possible. In this paper we developed and implemented washout algorithm, the results present the washout algorithm can improve the fidelity of flight simulator motion platform effectively.

### **II. 6-DOF PARALLEL MOTION PLATFORM**

Compared to series platforms, 6-dof parallel motion platform offer the advantages of high stiffness, speed capability, precision, low inertia at the expense of smaller workspace and ability to bear large loads [4]. So the 6-dof parallel motion platform have been used in military, industry and recreation result from its virtues.

Flight simulator is used to simulate the actual airplane on the ground. As an important part of flight simulator, the performance of the 6-dof parallel motion platform will directly affect the fidelity of flight simulation. Flight simulator with 6-dof parallel motion platform have the main outstanding virtues in reducing training costs, risks and improving training efficiency [5].

As the key parts of the 6-dof parallel motion platform, motion washout algorithm could compensate for the defects of flight simulator to enhance fidelity in flight simulation. Figure 1 is the structure drawing of a 6-dof parallel motion platform.

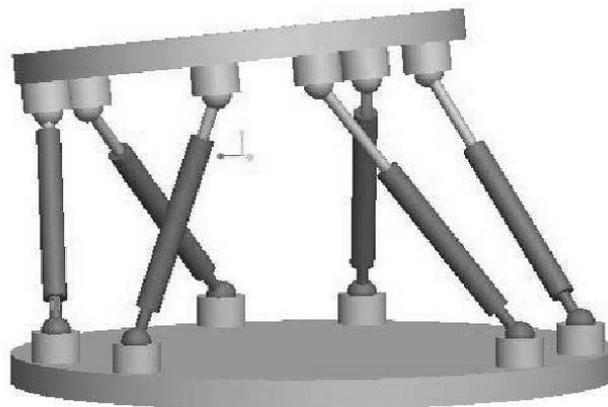


Fig -1: Schematic view of the 6-dof parallel motion platform

### 2.1 The Coordinate of 6-dof Parallel Motion Platform

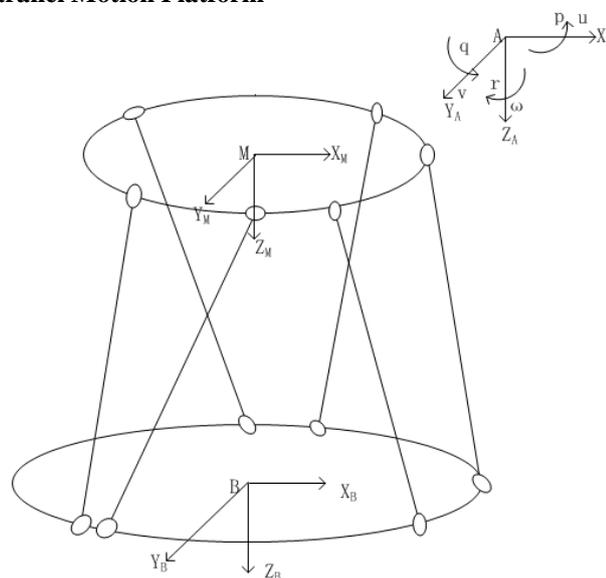


Fig -2: Frame assignment for the 6-dof parallel motion platform

The coordinate systems of 6-dof parallel motion platform has been constructed and illustrated in figure 2. The {B} coordinate system is the base coordinate system fixed to the base platform, the origin B of {B} is the geometry center of base platform, while the {M} is attached to the moving platform, the origin M of {M} is also the geometry center of moving platform. And cockpit systems coordinate is {A} with an origin A at the centroid of the cockpit. We assume the center of the vestibular system is fixed to the origin of cockpit systems coordinate in order to simplify calculation. All axes will be assumed to be orthogonal right hand axes, that is, positive forwards, positive right and positive down as shows in figure 2.

### 2.2 Translation Between Frames

The motion platform system needs to respond to the linear and angular accelerations like a real plane. The cockpit accelerations are transformed from the centroid of flight simulator cockpit to the pilot position and finally to the base frame in order to compute the actuator lengths. The cockpit accelerations and displacement of moving platform are filtered so that the moving platform motion never go beyond the maximum actuator displacements and the maximum actuator velocities.

Z-Y-X Euler angle is used to express the rotation matrix R from {A} to {B}. The linear velocities are  $u, v$  and  $w$ ; the angular velocities are  $p, q$  and  $r$  about the response  $x, y$  and  $z$  axes. Cockpit orientation about the cockpit systems coordinate can be defined as three angles, the path angle  $\theta$ , the roll angle  $\phi$  and the yaw angle  $\psi$ , known as Euler angles.

$$R = \begin{bmatrix} c\psi c\theta & c\psi s\theta s\phi - s\psi c\phi & c\psi s\theta c\phi + s\psi s\phi \\ s\psi c\theta & c\psi c\phi + s\psi s\theta s\phi & s\psi s\theta c\phi - c\psi s\phi \\ -s\theta & c\theta s\phi & c\theta c\phi \end{bmatrix} \quad (1)$$

Where,  $c=\cos$ ,  $s=\sin$ .

We need to translate the acceleration of A to the acceleration of B, is given by the transformation:

$$\bar{a}_b = R \bullet \bar{a} \quad (2)$$

Where  $\bar{a}_b$  is the acceleration of B and  $\bar{a}$  is the acceleration of A.

Cockpit orientation can be defined with respect to base coordinate, providing three angles, the path angle  $\theta_B$ , the roll angle  $\phi_B$  and the yaw angle  $\psi_B$ . The cockpit rates are given by:

$$\begin{bmatrix} p \\ q \\ r \end{bmatrix} = \begin{bmatrix} 1 & 0 & -\sin \theta \\ 0 & \cos \phi & \cos \theta \sin \phi \\ 0 & -\sin \phi & \cos \theta \cos \phi \end{bmatrix} \begin{bmatrix} \dot{\phi}_B \\ \dot{\theta}_B \\ \dot{\psi}_B \end{bmatrix} \quad (3)$$

The reverse transformation, to derive the Euler angle rates  $\omega_B$  from the cockpit rates, is given by the transformation:

$$\begin{bmatrix} \dot{\phi}_B \\ \dot{\theta}_B \\ \dot{\psi}_B \end{bmatrix} = \begin{bmatrix} 1 & \sin \theta \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi \sec \theta & \cos \phi \sec \theta \end{bmatrix} \begin{bmatrix} p \\ q \\ r \end{bmatrix} \quad (4)$$

### III. SIMULATION AND IMPLEMENTATION OF A MOTION SYSTEM

Acceleration sensation, linear and angular motion are provided by actuators attached between the moving platform and base platform. By providing strong initial motion sensation, the pilot is response to the change of velocity and acceleration. The wash-out filters can remove accelerations and restore the moving platform displacement to neutral position. Because of the mechanical limits of the motion platform, particularly the maximum actuator displacements and the maximum actuator velocities the motion platform needs to go back to the initial state after completing a flight behavior ,so that it is positioned to generate new motion sensations.

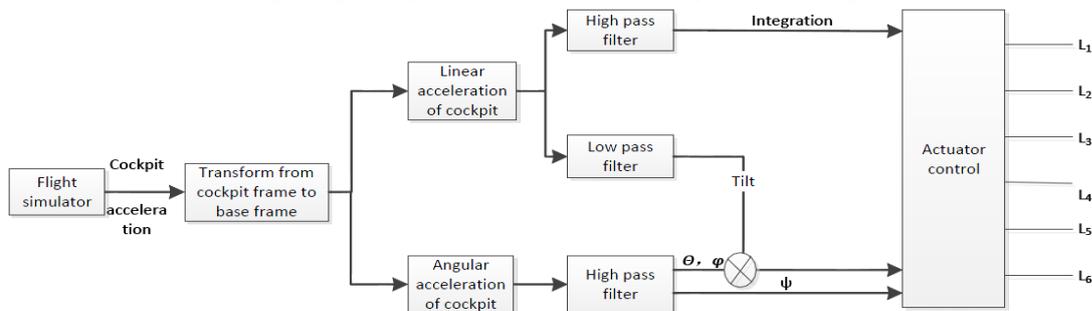


Fig -3: Schematic diagram of the motion washout algorithm

Figure 3 shows the schematic principle of motion washout algorithm. The high-pass filter responds to sudden changes to provide onset sensations as linear accelerations, but this motion reach the limits quickly. Sustained motion is represented through tilting the cabin that offers the gravitational acceleration vector. The relatively slow cabin motion as angular accelerations is achieved by the low-pass filter.

#### 3.1 The Washout Algorithm

The high-pass filter can be designed and implemented as a three-order system. As the velocity addition to maximum value, the acceleration needs to reduce to zero without pilot's sensation. As well, with the position of the actuator increases, the washout algorithm is used to reduce the platform acceleration and velocity to zero. The actuator position back to zero through the integrator. The effect of the high-pass filter is to offer the initial motionsensations, but to wash out these sensations before the actuator reaches its limited displacement.

The three-order form of filter is for high-pass filter of acceleration, and the two-order form of filter is for low-pass filter of acceleration and high-pass for angular velocity. Those are partly presented as below.

The three-order form of high-pass filter for acceleration is given by

$$\frac{x_h}{x_i} = \frac{k_1 s^2}{s^2 + 2\delta\omega_n s + \omega_n^2} \bullet \frac{s}{s + \omega_1} \quad (5)$$

Where  $x_i$  is the input position,  $x_h$  is the output position,  $\delta$  is the damping ratio,  $2\delta\omega_n$  corresponds to the viscous damping of the actuator.

The two-order form of low-pass filter for angular velocity is given by

$$\theta = k_2 \left( \frac{\omega^2}{s^2 + 2\delta\omega s + \omega^2} \right) \arctan \left( \frac{\ddot{x}_i}{g} \right) \quad (6)$$

$k_1$  and  $k_2$  are proportionality coefficient. We chose x axes direction to simulation and the value of different parameters are decided by debugging the motion washout algorithm repeatedly. Table 1 shows the value of algorithm parameters.

Table 1 parameters of washout algorithm

| Parameters | $k_1$ | $k_2$ | $\delta_{hx}$ | $\omega_{hx}$ | $\delta_{lx}$ | $\omega_{lx}$ |
|------------|-------|-------|---------------|---------------|---------------|---------------|
| Values     | 0.9   | 0.9   | 1             | 2.6           | 1             | 5             |

### 3.2 Simulation and Analysis

The effect of a high-pass filter on the platform motion is shown in Figure 4 to 6. Figure 4 is the vertical displacements. The toptrace shows vertical displacement of the cockpit which simulated an aircraft from horizontal flight to climb up. Figure 6 shows the moving platform longitudinal acceleration. The initial acceleration reaches 0.03 g before it is washed out. The longitudinal acceleration is washed out to zero without any sensations which proved the washout algorithm is effective. The moving platform displacement is approximately 19 in before it is washed out to zero as shown in figure 5. Notice that the moving platform does not exceed its limits of acceleration respectively, in the longitudinal axis. In fact, a higher-order filter is likely to be used to improve the response.

The motion system response with a low-pass filter is shown in Figure 7 and 8, for an applied yaw angular velocity increasing to 15 deg/sec after approximately 10 s. Figure 7 trace shows the yaw angular velocity through low pass filter and figure 8 trace shows yaw angle through low pass filter of the moving platform.

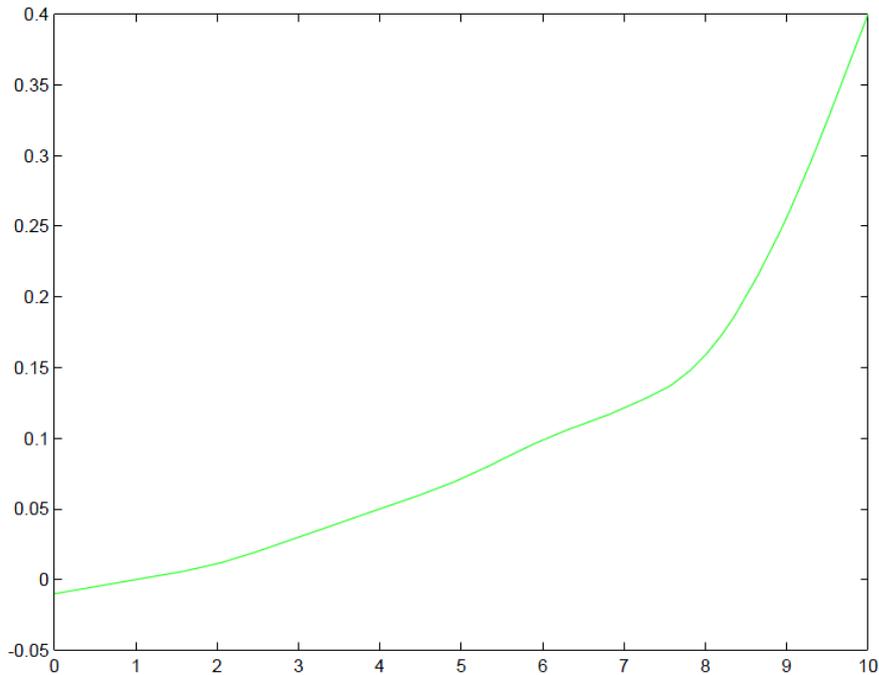
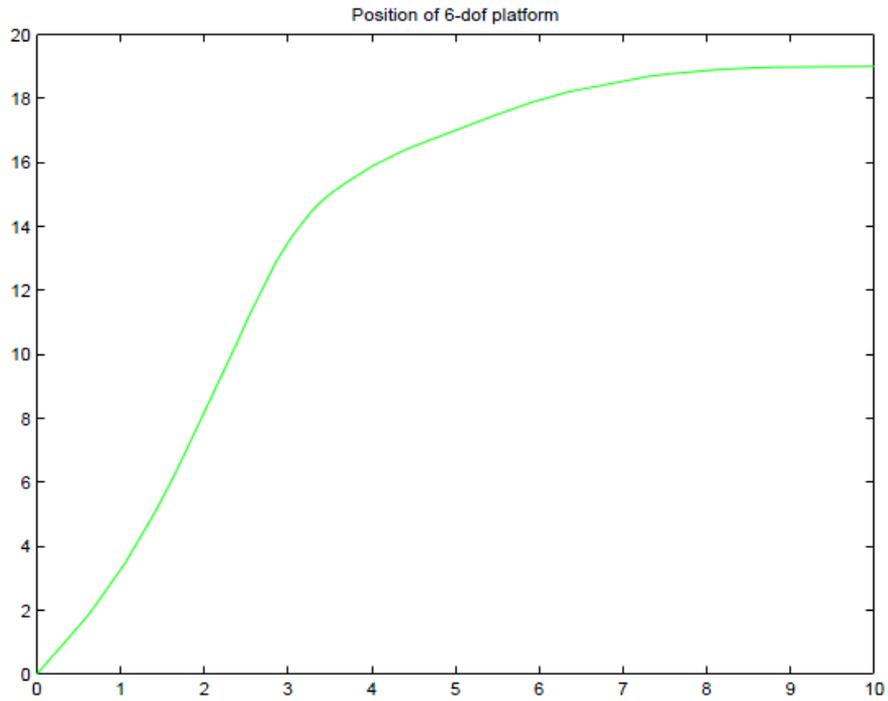
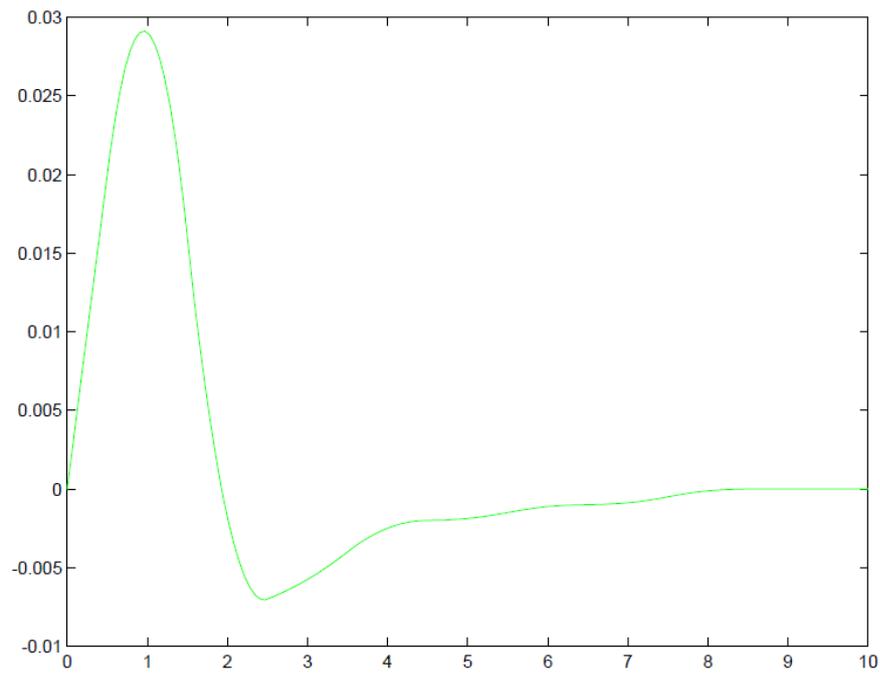


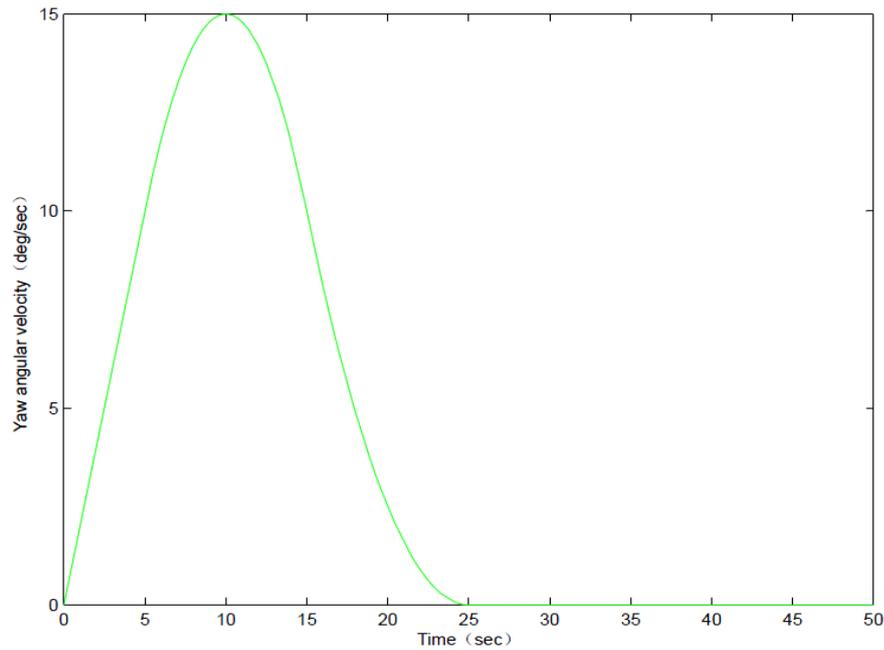
Fig -4: Vertical displacement



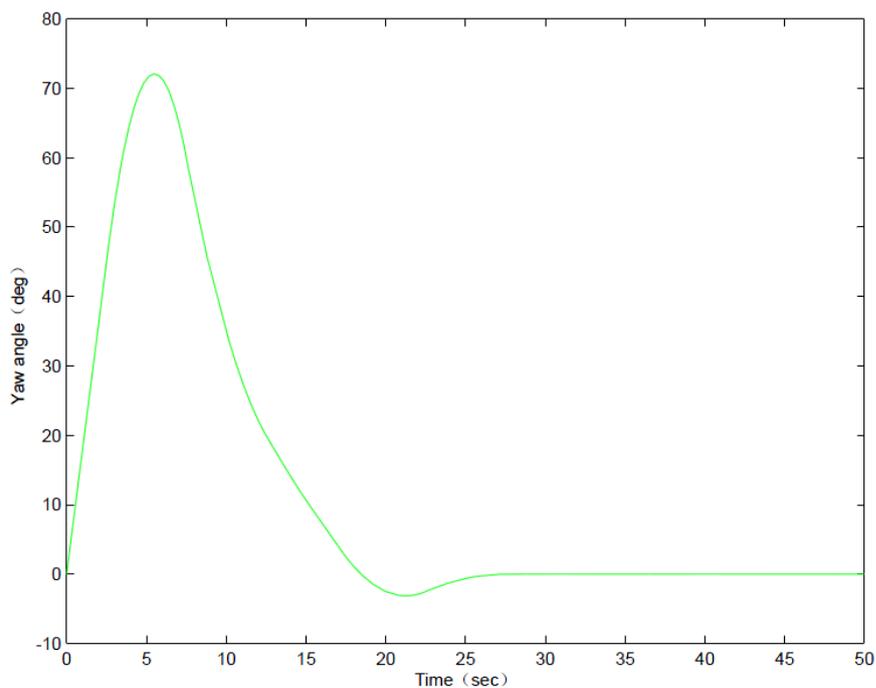
**Fig -5:** Position of 6-dof parallel platform



**Fig -6:** Longitudinal acceleration



**Fig -7:** Yaw angular velocity through low pass filter



**Fig -8:** Yaw angle through low pass filter

#### IV. CONCLUSIONS

In this paper we developed and implemented a classical washout algorithm which can simulate the actual aircraft with high fidelity. The developed washout algorithm can complete flight mission within limitation of the motion system. To overcome the signal distortion and the phase delay of the classical washout algorithm, we eliminated the low pass filter in tilt coordination algorithm. To attempt to replicate aircraft cues as accurately as possible, considerable effort is given to the selection of filter coefficients and the design of high-order algorithms. The washout algorithm was evaluated through computer simulation. It was verified that the developed washout algorithm is efficient. The washout algorithm should be improved with considerations of human sensation model and motion sensation recognized by pilot.

**REFERENCES**

- [1] Gao Z, Zhang D, Ge Y. Design optimization of a spatial six degree-of-freedom parallel manipulator based on artificial intelligence approaches. *Robotics and Computer-Integrated Manufacturing* 28(4), 2010, 484-92.
- [2] Ki Sung You, Min Cheol Lee, Eugene Kang, Wan Suk Yoo, Development of a Washout Algorithm for a Vehicle Driving Simulator Using New Tilt Coordination and Return Mode. *Journal of Mechanical Science and Technology* 19(1), 2005,272-282.
- [3] Grant, P.R., Reid, L.D.: Motion washout filter tuning: Rules and requirements. *Journal of Aircraft* 1997, 34(2), 145–151
- [4] Gianmarc Coppola, DanZhang, KefuLiu b. A 6-DOF reconfigurable hybrid parallel manipulator. *Robotics and Computer-Integrated Manufacturing* 30, 2014, 99-106.
- [5] X.M.GONG, X.H. LI and S.A.WANG. New motion cueing algorithm for driving simulator based on variant harmonic wavelet. *International Journal of Automotive Technology*16(1), 2015, 117-126.